wannier90: Tutorial

Version 1.2

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Preliminaries

Welcome to wannier90! The examples contained in this tutorial are designed to help you to become familiar with the procedure of generating, analysing and using maximally-localised Wannier functions (MLWF). As a first step, install wannier90 following the instructions in the README file of the wannier90 distribution. For an introduction to the theory underlying MLWF, you are encouraged to refer to the brief overview given in the wannier90 User Guide $[1]$, to the two seminal papers of Refs. $[2, 3]$, and to a recent paper $[4]$ describing wannier90.

The following additional programs should be installed in order to visualise the output of wannier90

- gnuplot is used to plot bandstructures. It is available for many operating systems and is often installed by default on unix/Linux distributions http://www.gnuplot.info
- xmgrace may also be used to plot bandstructures. http://plasma-gate.weizmann.ac.il/Grace
- XCrySDen is used to visualise crystal structures, MLWF, and Fermi surfaces. It is available for unix/Linux, Windows (using cygwin), and OSX. To correctly display files from wannier90, version 1.4 or later must be used. http://www.xcrysden.org
- vmd can also be used to visualise crystal structures and MLWF. http://www.ks.uiuc.edu/Research/vmd

About this tutorial

The first part of this tutorial comprises four examples taken from Refs. [2, 3]: gallium arsenide, lead, silicon and copper. All of the wannier90 input files have been provided.

The second part of the tutorial covers the generation of wannier90 input files starting from a full electronic structure calculation. We have provided input files for the PWSCF

(www.quantum-espresso.org) interface to wannier90. Therefore, you will need to install and compile elements of the quantum-espresso package, namely $pw.x$ and $pw2w$ annier 90.x, in order to run these examples. Please visit www.quantum-espresso.org to download the package, and for installation instructions.

At the time of writing, interfaces to a number of other electronic structure codes, such as castep (www.castep.org), abinit (www.abinit.org), and fleur (www.flapw.de), are in progress.

For images of MLWF, see our gallery at http://www.wannier.org/gallery.html. If you have any images that you would like to submit to the gallery, please email us.

Contact us

If you have any suggestions regarding ways in which this tutorial may be improved, then send us an email.

For other questions, email the wannier90 forum at wannier@quantum-espresso.org. Note that first you will need to register in order to post emails. Emails from non-registered users are deleted automatically. You can register by following the links at http://www.wannier.org/forum.html.

1: Gallium Arsenide

- Outline: *Obtain and plot MLWF for the four valence bands of GaAs.*
- Generation details: From PWSCF, using norm-conserving pseudopotentials and a $2 \times 2 \times 2$ k-point grid. Starting guess: four bond-centred Gaussians.
- Directory: examples/example1/
- Input Files
	- $-$ gaas.win The master input file
	- gaas.mmn The overlap matrices $M^{(k,b)}$
	- gaas.amn Projection $A^{(k)}$ of the Bloch states onto a set of trial localised orbitals
	- UNK00001.1 The Bloch states in the real space unit cell. For plotting only.
- 1. Run wannier90 to minimise the MLWF spread

```
wannier90.x gaas
```
Inspect the output file gaas.wout. The total spread converges to its minimum value after just a few iterations. Note that the geometric centre of each MLWF lies along a Ga-As bond, slightly closer to As than Ga. Note also that the memory requirement for the minimisation of the spread is very low as the MLWF are defined at each k-point by just the 4×4 unitary matrices $\mathbf{U}^{(\mathbf{k})}$.

2. Plot the MLWF by adding the following keywords to the input file gaas.win

wannier plot = true

and re-running wannier90. To visualise the MLWF we must represent them explicitly on a real space grid (see Ref. [1]). As a consequence, plotting the MLWF is slower and uses more memory than the minimisation of the spread. The four files that are created $(gaas_00001.xsf, etc.)$ can be viewed using XCrySDen,¹ e.g.,

xcrysden --xsf gaas_00001.xsf

For large systems, plotting the MLWF may be time consuming and require a lot of memory. Use the keyword wannier plot list to plot a subset of the MLWF. E.g., to plot the 1st, 2nd and 7th MLWF use

```
wannier plot list = 1 2 7
```
The MLWF are plotted in a supercell of the unit cell. The size of this supercell is set through the keyword wannier plot supercell. The default value is 2 (corresponding to a supercell with eight times the unit cell volume). We recommend not using values great than 3 as the memory and computational cost scales cubically with supercell size.

Plot the 3rd MLWF in a supercell of size 3. Choose a low value for the isosurface (say 0.5). Can you explain what you see?

¹Once XCrySDen starts, click on Tools \rightarrow Data Grid in order to specify an isosurface value to plot.

Hint: For a finite k-point mesh, the MLWF are in fact periodic and the period is related to the spacing of the k-point mesh. For mesh with n divisions in the ith direction in the Brillouin zone, the MLWF "live" in a supercell n times the unit cell.

2: Lead

- Outline: *Obtain MLWF for the four lowest states in lead. Use Wannier interpolation* to plot the Fermi surface
- Generation Details: From pwscf, using norm-conserving pseudopotentials and a $4 \times 4 \times 4$ k-point grid. Starting guess: atom-centred sp^3 hybrid orbitals
- Directory: examples/example2/
- Input Files
	- $-$ lead.win The master input file
	- lead.mmn The overlap matrices $\mathbf{M}^{(\mathbf{k},\mathbf{b})}$
	- lead.amn Projection $A^{(k)}$ of the Bloch states onto a set of trial localised orbitals
	- lead.eig The Bloch eigenvalues at each k-point. For interpolation only

The four lowest valence bands in lead are separated in energy from the higher conduction states (see Fig. 1). The MLWF of these states have partial occupancy. MLWF describing only the occupied states would be poorly localised.

1. Run wannier90 to minimise the MLWF spread

wannier90.x lead

Inspect the output file lead.wout.

2. Use Wannier interpolation to obtain the Fermi surface of lead. Rather than re-running the whole calculation we can use the unitary transformations obtained in the first calculation and restart from the plotting routine. Add the following keywords to the lead.win file:

```
restart = plot
fermi\_energy = 5.2676fermi surface plot = true
```
and re-run wannier90. The value of the Fermi energy (5.2676 eV) was obtained from the initial first principles calculation. wannier90 calculates the band energies, through wannier interpolation, on a dense mesh of k-points in the Brillouin zone. The density of this grid is controlled by the keyword fermi surface num points. The default value is 50 (i.e., 50^3 points). The Fermi surface file lead.bxsf can be viewed using XCrySDen, e.g.,

xcrysden --bxsf lead.bxsf

Figure 1: Bandstructure of lead showing the position of the Fermi level. Only the lowest four bands are included in the calculation.

3: Silicon

- Outline: *Obtain MLWF* for the valence and low-lying conduction states of Si. Plot the interpolated bandstructure
- Generation Details: From pwscf, using norm-conserving pseudopotentials and a $4 \times 4 \times 4$ k-point grid. Starting guess: atom-centred sp^3 hybrid orbitals
- Directory: examples/example3/
- Input Files
	- $-$ silicon.win The master input file
	- silicon.mmn The overlap matrices $\mathbf{M^{(k,b)}}$
	- silicon.amn Projection $A^{(k)}$ of the Bloch states onto a set of trial localised orbitals
	- $-$ silicon.eig The Bloch eigenvalues at each k-point

The valence and lower conduction states can be represented by MLWF with sp³-like symmetry. The lower conduction states are not separated from the higher states by an energy gap. In order to form localised WF, we use the disentanglement procedure introduced in Ref. [3]. The position of the inner and outer energy windows are shown in Fig. 2.

1. Run wannier90.

wannier90.x silicon

Inspect the output file silicon.wout. The minimisation of the spread occurs in a twostep procedure [3]. First, we minimise Ω_I – this is the extraction of the optimal subspace in the disentanglement procedure. Then, we minimise $\Omega_{\rm D} + \Omega_{\rm OD}$.

2. Plot the MLWF by adding the following commands to the input file silicon.win

```
restart = plot
bands_plot = true
```
and re-running wannier90. The files silicon_band.dat and silicon_band.gnu are created. To plot the bandstructure using gnuplot

myshell> gnuplot gnuplot> load 'silicon band.gnu'

The k-point path for the bandstructure interpolation is set in the kpoint path block. Try plotting along different paths.

Figure 2: Bandstructure of silicon showing the position of the outer and inner energy windows.

4: Copper

- Outline: *Obtain MLWF to describe the states around the Fermi-level in copper*
- Generation Details: From PWSCF, using ultrasoft pseudopotentials [5] and a $4 \times 4 \times 4$ k-point grid. Starting guess: five atom-centred d orbitals, and two s orbitals centred on one of each of the two tetrahedral interstices.
- Directory: examples/example4/
- Input Files
	- $-$ copper.win The master input file
	- copper.mmn The overlap matrices $M^{(k,b)}$
	- copper. amn Projection $A^{(k)}$ of the Bloch states onto a set of trial localised orbitals
	- $-$ copper.eig The Bloch eigenvalues at each k-point
- 1. Run wannier90 to minimise the MLWF spread

```
wannier90.x copper
```
Inspect the output file copper.wout.

- 2. Plot the Fermi surface, it should look familiar! The Fermi energy is at 12.2103 eV.
- 3. Plot the interpolated bandstructure. A suitable path in k-space is

begin kpoint path G 0.00 0.00 0.00 X 0.50 0.50 0.00 X 0.50 0.50 0.00 W 0.50 0.75 0.25 W 0.50 0.75 0.25 L 0.00 0.50 0.00 L 0.00 0.50 0.00 G 0.00 0.00 0.00 G 0.00 0.00 0.00 K 0.00 0.50 -0.50 end kpoint_path

4. Plot the contribution of the interstitial WF to the bandstructure. Add the following keyword to copper.win

bands_plot_project = $6,7$

The resulting file copper band proj.gnu can be opened with gnuplot. Red lines correspond to a large contribution from the interstitial WF (blue line are a small contribution; ie a large 'd' contribution).

Investigate the effect of the outer and inner energy window on the interpolated bands.

Figure 3: Bandstructure of copper showing the position of the outer and inner energy windows.

Examples Using the PWSCF Interface

The PWSCF plane-wave, density-functional theory code, which is available as part of the quantum-espresso distribution (www.quantum-espresso.org), is fully interfaced to wannier90 via the pw2wannier90 post-processing code that is also available as part of QUANTUMespresso. The latest version of pw2wannier90 is included as part of the wannier90 distribution. Please see the pwscf directory for instructions on how to incorporate it into pwscf.

5: Diamond

- Outline: *Obtain MLWF for the valence bands of diamond*
- Directory: examples/example5/
- Input Files
	- $-$ diamond.scf The PWSCF input file for ground state calculation
	- $-$ diamond.nscf The PWSCF input file to obtain Bloch states on a uniform grid
	- $-$ diamond.pw2wan The input file for pw2wannier90
	- diamond.win The wannier90 input file
- 1. Run PWSCF to obtain the ground state of diamond pw.x < diamond.scf > scf.out
- 2. Run PWSCF to obtain the Bloch states on a uniform k-point grid pw.x < diamond.nscf > nscf.out
- 3. Run wannier90 to generate a list of the required overlaps (written into the diamond.nnkp file). wannier90.x -pp diamond
- 4. Run pw2wannier90 to compute the overlap between Bloch states and the projections for the starting guess (written in the diamond.mmn and diamond.amn files). pw2wannier90.x < diamond.pw2wan > pw2wan.out
- 5. Run wannier90 to compute the MLWF. wannier90.x diamond

6: Copper

- Outline: *Obtain MLWF to describe the states around the Fermi-level in copper*
- Directory: examples/example6/
- Input Files
	- $-$ copper.scf The PWSCF input file for ground state calculation
	- $-$ copper.nscf The PWSCF input file to obtain Bloch states on a uniform grid
	- copper.pw2wan $Input$ file for pw2wannier90
	- copper.win The wannier90 input file
- 1. Run PWSCF to obtain the ground state of copper pw.x < copper.scf > scf.out
- 2. Run PWSCF to obtain the Bloch states on a uniform k-point grid pw.x < copper.nscf > nscf.out
- 3. Run wannier90 to generate a list of the required overlaps (written into the copper.nnkp file). wannier90.x -pp copper
- 4. Run pw2wannier90 to compute the overlap between Bloch states and the projections for the starting guess (written in the copper.mmn and copper.amn files). pw2wannier90.x < copper.pw2wan > pw2wan.out
- 5. Run wannier90 to compute the MLWF. wannier90.x copper

Inspect the output file copper.wout.

1. Use Wannier interpolation to obtain the Fermi surface of copper. Rather than rerunning the whole calculation we can use the unitary transformations obtained in the first calculation and restart from the plotting routine. Add the following keywords to the copper.win file:

```
restart = plot
fermi energy = [insert your value here]
fermi surface plot = true
```
and re-run wannier90. The value of the Fermi energy can be obtained from the initial first principles calculation. wannier90 calculates the band energies, through wannier interpolation, on a dense mesh of k-points in the Brillouin zone. The density of this grid is controlled by the keyword fermi surface num points. The default value is 50 (i.e., $50³$ points). The Fermi surface file copper.bxsf can be viewed using XCrySDen, e.g.,

xcrysden --bxsf copper.bxsf

2. Plot the interpolated bandstructure. A suitable path in k-space is

begin kpoint path G 0.00 0.00 0.00 X 0.50 0.50 0.00 X 0.50 0.50 0.00 W 0.50 0.75 0.25 W 0.50 0.75 0.25 L 0.00 0.50 0.00 L 0.00 0.50 0.00 G 0.00 0.00 0.00 G 0.00 0.00 0.00 K 0.00 0.50 -0.50 end kpoint_path

Further ideas

- $\bullet\,$ Compare the Wannier interpolated bandstructure with the full <code>pwscf</code> bandstructure. Obtain MLWF using a more dense k-point grid.
- Investigate the effect of the outer and inner energy window on the interpolated bands.
- Instead of extracting a subspace of seven states, we could extract a nine dimensional space (i.e., with s, p and d character). Examine this case and compare the projected bandstructures.

7: Silane - SiH_4

- Outline: *Obtain MLWF for the occupied states of molecular silane.* Γ-*point sampling*
- Directory: examples/example7/
- Input Files
	- $-$ silane.scf The PWSCF input file for ground state calculation
	- $-$ silane.nscf The PWSCF input file to obtain Bloch states on a uniform grid
	- $-$ silane.pw2wan $Input$ file for pw2wannier90
	- silane.win The wannier90 input file
- 1. Run PWSCF to obtain the ground state of silane pw.x < silane.scf > scf.out
- 2. Run PWSCF to obtain the Bloch states on a uniform k-point grid pw.x < silane.nscf > nscf.out
- 3. Run wannier90 to generate a list of the required overlaps (written into the silane.nnkp file). wannier90.x -pp silane
- 4. Run pw2wannier90 to compute the overlap between Bloch states and the projections for the starting guess (written in the silane.mmn and silane.amn files). pw2wannier90.x < silane.pw2wan > pw2wan.out
- 5. Run wannier90 to compute the MLWF. wannier90.x silane

8: Iron

- Outline: *Obtain MLWF to describe the states around the Fermi-level in iron.*
- Directory: examples/example8/
- Input Files
	- $-$ iron.scf The PWSCF input file for ground state calculation
	- $-$ iron.nscf The PWSCF input file to obtain Bloch states on a uniform grid
	- $-$ iron up.pw2wan Input file for pw2wannier90 spin up
	- $-$ iron_up.win The wannier90 input file spin up
	- $-$ iron_dn.pw2wan $Input$ file for pw2wannier90 spin down
	- $-$ iron_dn.win The wannier90 input file spin down
- Note that we obtain the MLWF for spin up and spin down in separate calculations.
- 1. Run PWSCF to obtain the ground state of iron pw.x < iron.scf > scf.out
- 2. Run PWSCF to obtain the Bloch states on a uniform k-point grid pw.x < iron.nscf > nscf.out
- 3. Run wannier90 to generate a list of the required overlaps (written into the iron up.nnkp and iron_dn.nnkp files). wannier90.x -pp iron_up

wannier90.x -pp iron_dn

4. Run pw2wannier90 to compute the overlap between Bloch states and the projections for the starting guess (written in the iron up.mmn, iron dn.mmn, iron up.amn and iron dn.amn files).

pw2wannier90.x < iron up.pw2wan > pw2wan.out pw2wannier90.x < iron dn.pw2wan > pw2wan.out

5. Run wannier90 to compute the MLWF. wannier90.x iron_up wannier90.x iron dn

9: Cubic BaTi O_3

- Outline: Obtain MLWF for a perovskite
- Directory: examples/example9/
- Input Files
	- $-$ batio3.scf The PWSCF input file for ground state calculation
	- $-$ batio3.nscf The PWSCF input file to obtain Bloch states on a uniform grid
	- $-$ batio3.pw2wan $Input$ file for pw2wannier90
	- $-$ batio3.win The wannier90 input file

To start with, we are going to obtain MLWF for the oxygen 2p states. From the bandstructure [6], these form an isolated group of bands. We use the wannier90 keyword exclude bands to remove all but the 2p bands from the calculation of the overlap and projection matrices (we don't have to do this, but it saves time).

- 1. Run PWSCF to obtain the ground state of $BaTiO₃$ pw.x < BaTiO3.scf > scf.out
- 2. Run PWSCF to obtain the Bloch states on a uniform k-point grid pw.x < BaTiO3.nscf > nscf.out
- 3. Run wannier90 to generate a list of the required overlaps (written into the BaTiO3.nnkp file).

wannier90.x -pp BaTiO3

- 4. Run pw2wannier90 to compute the overlap between Bloch states and the projections for the starting guess (written in the BaTiO3.mmn and BaTiO3.amn files). pw2wannier90.x < BaTiO3.pw2wan > pw2wan.out
- 5. Run wannier90 to compute the MLWF. wannier90.x BaTiO3

Inspect the output file BaTiO3.wout.

Plot the second MLWF, as described in Section 1, by adding the following keywords to the input file BaTiO3.win

```
wannier plot = true
restart = plot
wannier plot list = 2
wannier_plot_supercell = 3
```
and re-running wannier90. Visualise it using XCrySDen,

xcrysden --xsf BaTiO3 00002.xsf

We can now simulate the ferroelectric phase by displacing the Ti atom. Change its position to

Ti 0.505 0.5 0.5

and regenerate the MLWF (i.e., compute the ground-state charge density and Bloch states using PWSCF, etc.) and look at the change in the second MLWF.

Further ideas

- Look at MLWF for other groups of bands. What happens if you form MLWF for the whole valence manifold?
- Following Ref. [6], compute the Born effective charges from the change in Wannier centres under an atomic displacement.

10: Graphite

- Outline: *Obtain MLWF for graphite (AB, Bernal)*
- Directory: examples/example10/
- Input Files
	- $-$ graphite.scf The PWSCF input file for ground state calculation
	- $-$ graphite.nscf The PWSCF input file to obtain Bloch states on a uniform grid
	- $-$ graphite.pw2wan $Input$ file for pw2wannier90
	- graphite.win The wannier90 input file
- 1. Run PWSCF to obtain the ground state of graphite pw.x < graphite.scf > scf.out
- 2. Run PWSCF to obtain the Bloch states on a uniform k-point grid pw.x < graphite.nscf > nscf.out
- 3. Run wannier 90 to generate a list of the required overlaps (written into the graphite.nnkp file). wannier90.x -pp graphite
- 4. Run pw2wannier90 to compute the overlap between Bloch states and the projections for the starting guess (written in the graphite.mmn and graphite.amn files). pw2wannier90.x < graphite.pw2wan > pw2wan.out
- 5. Run wannier90 to compute the MLWF. wannier90.x graphite

11: Silicon

Valence Bands

- Outline: *Obtain MLWF for the valence bands of silicon*
- Directory: examples/example11/
- Input Files
	- $-$ silicon.scf The PWSCF input file for ground state calculation
	- $-$ silicon.nscf The PWSCF input file to obtain Bloch states on a uniform grid
	- $-$ silicon.pw2wan $Input$ file for pw2wannier90
	- $-$ silicon.win The wannier90 input file
- 1. Run PWSCF to obtain the ground state of silicon pw.x < silicon.scf > scf.out
- 2. Run pwscf to obtain the Bloch states on a uniform k-point grid. Note that we request the lower 4 (valence) bands pw.x < silicon.nscf > nscf.out
- 3. Run wannier 90 to generate a list of the required overlaps (written into the silicon.nnkp file).

wannier90.x -pp silicon

- 4. Run pw2wannier90 to compute the overlap between Bloch states and the projections for the starting guess (written in the silicon.mmn and silicon.amn files). pw2wannier90.x < silicon.pw2wan > pw2wan.out
- 5. Run wannier90 to compute the MLWF. wannier90.x silicon

Inspect the output file silicon.wout. The total spread converges to its minimum value after just a few iterations. Note that the geometric centre of each MLWF lies at the centre of the Si-Si bond. Note also that the memory requirement for the minimisation of the spread is very low as the MLWF are defined by just the 4×4 unitary matrices $\mathbf{U}^{(\mathbf{k})}$.

Plot the MLWF by adding the following keywords to the input file silicon.win

wannier plot = true

and re-running wannier90. Visualise them using XCrySDen, e.g.,

xcrysden --xsf silicon 00001.xsf

Valence + Conduction State

- Outline: *Obtain MLWF for the valence and low-lying conduction states of Si. Plot the* interpolated bandstructure
- Input Files
	- $-$ silicon.scf The PWSCF input file for ground state calculation
	- $-$ silicon.nscf The PWSCF input file to obtain Bloch states on a uniform grid
	- $-$ silicon.pw2wan $Input$ file for pw2wannier90
	- $-$ silicon.win The wannier90 input file

The valence and lower conduction states can be represented by MLWF with sp³-like symmetry. The lower conduction states are not separated by an energy gap from the higher states. In order to form localised WF we use the disentanglement procedure introduced in Ref. [3]. The position of the inner and outer energy windows are shown in Fig. 2.

- 1. Modify the input file and run PWSCF and wannier90. Inspect the output file silicon.wout. The minimisation of the spread occurs in a twostep procedure. First, we minimise Ω_I – this is the extraction of the optimal subspace in the disentanglement procedure. Then, we minimise $\Omega_{\text{O}} + \Omega_{\text{OD}}$.
- 2. Plot the bandstructure by adding the following commands to the input file silicon.win

```
restart = plot
bands_plot = true
```
and re-running wannier90. The files silicon band.dat and silicon band.gnu are created. To plot the bandstructure using gnuplot

```
myshell> gnuplot
gnuplot> load 'silicon band.gnu'
```
The k-point path for the bandstructure interpolation is set in the kpoint path block. Try plotting along different paths.

Further ideas

- Compare the Wannier interpolated bandstructure with the full PWSCF bandstructure. Compute MLWF using a finer k-point grid (e.g., $6\times6\times6$ or $8\times8\times8$) and note how the accuracy of the interpolation increases [7].
- Compute MLWF for four conduction states (see Ref. [3]).

12: Benzene

Valence States

- Outline: Obtain MLWF for the valence states of benzene
- Directory: examples/example12/
- Input Files
	- $-$ benzene.scf The PWSCF input file for ground state calculation
	- benzene.pw2wan $Input file for$ pw2wannier90
	- benzene.win The wannier90 input file
- 1. Run PWSCF to obtain the ground state of benzene pw.x < benzene.scf > scf.out
- 2. Run wannier90 to generate a list of the required overlaps (written into the benzene.nnkp file). wannier90.x -pp benzene
- 3. Run pw2wannier90 to compute the overlap between Bloch states and the projections for the starting guess (written in the benzene.mmn and benzene.amn files). pw2wannier90.x < benzene.pw2wan > pw2wan.out
- 4. Run wannier90 to compute the MLWF. wannier90.x benzene

Inspect the output file benzene.wout. The total spread converges to its minimum value after just a few iterations.

Plot the MLWF by adding the following keywords to the input file benzene.win

restart = plot wannier plot = true wannier plot format = cube wannier plot list = 2-4

and re-running wannier90. Visualise them using, e.g., XCrySDen.

Valence + Conduction States

- Outline: Obtain MLWF for the valence and low-lying conduction states of benzene.
- Input Files
	- $-$ benzene.scf The PWSCF input file for ground state calculation
- $-$ benzene.nscf The pwscf input file to obtain Bloch states for the conduction states
- benzene.pw2wan $Input$ file for pw2wannier90
- benzene.win The wannier90 input file

In order to form localised WF we use the disentanglement procedure. The position of the inner energy window is set to lie in the energy gap; the outer energy window is set to 4.0 eV. Modify the input file appropriately.

- 1. Run PWSCF and wannier90. Inspect the output file benzene.wout. The minimisation of the spread occurs in a two-step procedure. First, we minimise Ω_{I} . Then, we minimise $\Omega_{\text{O}} + \Omega_{\text{OD}}$.
- 2. Plot the MLWF by adding the following commands to the input file benzene.win

restart = plot wannier plot = true wannier plot format = cube $wannier_plot_list = 1,7,13$

and re-running wannier90. Visualise them using, e.g., XCrySDen.

13: (5,5) Carbon Nanotube

Transport properties

- Outline: *Obtain the bandstructure, quantum conductance and density of states of a* metallic (5,5) carbon nanotube
- Directory: examples/example13/
- Input Files
	- $-$ cnt55.scf The PWSCF input file for ground state calculation
	- $-$ cnt55.nscf The PWSCF input file to obtain Bloch states for the conduction states
	- $-$ cnt55.pw2wan Input file for pw2wannier90
	- $-$ cnt55.win The wannier90 input file

In order to form localised WF that describe both the occupied and unoccupied π and π^* manifolds, we use the disentanglement procedure to extract a smooth manifold of states that has dimension equal to 2.5 times the number of carbon atoms per unit cell [8]. The positions of the energy windows are shown in Fig. 4.

The part of the wannier90 input file that controls the transport part of the calculation looks like:

```
transport = true
transport mode = bulk
one_dim_axis = zdist_cutoff = 5.5fermi_energy = -1.06tran_win_min = -6.5tran\_win\_max = 6.5tran_{energy\_step} = 0.01dist cutoff mode = one dim
translation centre frac = 0.0 0.0 0.0
```
Descriptions of these and other keywords related to the calculation of transport properties can be found in the User Guide.

1. Run PWSCF and wannier90. Inspect the output file cnt55.wout. The minimisation of the spread occurs in a two-step

procedure. First, we minimise Ω_{I} . Then, we minimise $\Omega_{\text{O}} + \Omega_{\text{OD}}$.

- 2. Note that the initial p_z projections on the carbon atoms are oriented in the radial direction with respect to the nanotube axis.
- 3. The interpolated bandstructure is written to cnt55-band age (since bands plot format = xmgr in the input file).

4. The quantum conductance and density of states are written to the files cnt55 qc.dat and cnt55 dos.dat, respectively. Note that this part of the calculation may take some time. You can follow its progress by monitoring the output to these files. Use a package such as gnuplot or xmgrace in order to visualise the data. You should get something that looks like Fig. 5.

Figure 4: Bandstructure of (5,5) carbon nanotube showing the position of the outer and inner energy windows.

Figure 5: Wannier interpolated bandstructure, quantum conductance and density of states of (5,5) carbon nanotube. Note that the Fermi level has been shifted by 1.06eV with respect to Fig. 4.

14: Linear Sodium Chain

- Outline: *Compare the quantum conductance of a periodic linear chain of Sodium atoms* with that of a defected chain
- Directories: examples/example14/periodic examples/example14/defected
- Input Files
	- $-$ Na_{chain}.scf The PWSCF input file for ground state calculation
	- $-$ Na_{chain}.nscf The pwscf input file to obtain Bloch states for the conduction states
	- Na_chain.pw2wan $Input$ file for <code>pw2wannier90</code>
	- Na_chain.win The wannier90 input file

The periodic system is contians two unit cells evenly distributed along the supercell. Transport calculations are performed using transport mode = bulk and so the resulting quantum conductance represents that of an infinite periodic chain.

The part of the wannier90 input file that controls the transport part of the calculation looks like:

```
transport = true
transport mode = bulk
tran read ht = false
one dim axis = xfermi_{energy} = -2.7401tran\_win\_min = -5.0tran\_win\_max = 5.0tran_{energy\_step} = 0.01translation centre frac = 0.5 0.5 0.5
tran_number = 2
```
The defected system uses a 13 atom supercell with the central atom position altered to break symmetry. Setting transport mode = lcr with tell wannier90 to treat the system as an infinte sytsem with the defect at its centre. The supercell is chosen so that is conforms to the 2c2 geometry (see User Guide for details). Each principal layer is 2 atoms long so that the conductor region contains the defected atom plus a single atom on either side.

The transport section of the input file contians these key differences:

transport mode = lcr $tran_number = 2$ $tran_number$ $11 = 2$

Descriptions of these and other keywords related to the calculation of transport properties can be found in the User Guide.

- 1. Run PWSCF and wannier90 for the periodic system.
- 2. Run PWSCF and wannier90 for the defected system.
- 3. The quantum conductance is written to the files periodic/Na chain qc.dat and defected/Na chain dos.dat, respectively. Compare the quantum conductance of the periodic (bulk) calculation with the defected (LCR) calculation. Your plot should look like Fig. 6.

Figure 6: Quantum conductance of periodic Sodium chain (black) compared to that of the defected Sodium chain (red).

15: (5,0) Carbon Nanotube

Note that these systems require reasonably large-scale electronic structure calculations.

Bulk Transport properties

- Outline: *Obtain the quantum conductance of a pristine single-walled carbon nanotube*
- Directory: examples/example14/periodic
- Input Files
	- $-$ cnt.scf The PWSCF input file for ground state calculation
	- $-$ cnt.nscf The PWSCF input file to obtain Bloch states for the conduction states
	- $-$ cnt.pw2wan $Input$ file for pw2wannier90
	- cnt.win The wannier 90 input file

First we consider a single unit cell, with 10 k-points. With transport mode = bulk we compute the transport properties of a pristine, infinite, periodic (5,0) carbon nanotube. Later, we will compare the quantum conductance of this system with a defected nanotube.

- 1. Run PWSCF and wannier90.
- 2. The quantum conductance and density of states are written to the files cnt qc.dat and cnt dos.dat, respectively.

LCR transport properties – Defected nanotube

- Outline: Use the automated LCR routine to investigate the effect of a single silicon atom in a infinite $(5,0)$ carbon nanotube.
- Directory: examples/example15/defected
- Input Files
	- $-$ cnt+si.scf The PWSCF input file for ground state calculation
	- $-$ cnt+si.nscf The PWSCF input file to obtain Bloch states for the conduction states
	- $-$ cnt+si.pw2wan $Input$ file for pw2wannier90
	- cnt+si.win The wannier90 input file

In this calculation a 11 atom supercell is used with a single silicon substitutional defect in the central unit cell. The supercell is chosen so that is conforms to the 2c2 geometry (see User Guide for details) with principal layers set to be 2 unit cells long.

- 1. Run pwscf and wannier90. Again these are large calculations, progress can be monitored by viewing respective output files.
- 2. The quantum conductance is written to cnt+si qc.dat. Compare the quantum conductance with the periodic (bulk) calculation. Your plot should look like Fig. 7.

Figure 7: Quantum conductance of infinite pristine nanotube (black) compared to that of the infinite nanotube with the substitutional silicon defect (red).

Further ideas

- Set $hr.plot = true$ in the bulk case. Consider the magnitude of Hamiltonian elements between Wannier functions in increasingly distant unit cells. Are two unit cell principal layers really large enough, or are significant errors introduced?
- Does one unit cell either side of the defected unit cell shield the disorder so that the leads are ideal? Does the quantum conductance change if these 'buffer' regions are increased?

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