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# Monovacancy-induced magnetism in graphene bilayers

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#### **Abstract**

Vacancy-induced magnetism in graphene bilayers is investigated using spin-polarized density functional theory calculations. One of two graphene layers has a monovacancy. Two atomic configurations for bilayers are considered with respect to the position of the monovacancy. We find that spin magnetic moments localized at the vacancy site decrease by  $\sim \! 10\%$  for our two configurations, compared with the graphene monolayer with a monovacancy. The reduction of the spin magnetic moment in the graphene bilayers is attributed to the interlayer charge transfer from the adjacent layer to the layer with the monovacancy, compensating for spin magnetic moments originating from quasilocalized defect states.

(Some figures in this article are in colour only in the electronic version)

# 1. Introduction

Vacancy defects in crystalline solids have been of fundamental interest in materials science and condensed matter physics. Of particular interest, both technologically and academically, are the vacancy defects in nanostructures of sp<sup>2</sup>-bonded They exhibit roomcarbon-based nanostructures [1, 2]. temperature (RT) ferromagnetism [3], and the underlying physics of their ferromagnetism is different from that of conventional ferromagnetic metals such as iron and cobalt [4, 5]. Successive progress in the understanding of ferromagnetism in carbon-based nanostructures has been achieved by theoretical approaches based on spin-polarized density functional theory [6-9] and experiments on irradiated carbon nanostructures [10-12]. To illustrate, for a graphene monolayer (a two-dimensional honeycomb lattice of C atoms) with a monovacancy, it has been elucidated that spin magnetic moment is localized at the vacancy site and that RTferromagnetism in the graphene monolayer originates from a localized sp<sup>2</sup> dangling bond state as well as a quasilocalized defect state [4, 13].

Previous theoretical studies of magnetism in twodimensional graphitic systems have focused on the graphene monolayer, neglecting the interlayer coupling. In this paper, we investigate, using first-principles calculations, graphene bilayers with a monovacancy to understand the influence of the adjacent graphene layer on the spin magnetic moment of the graphene layer with a monovacancy. This result would provide a more realistic understanding of vacancy-induced magnetism in graphene multilayer systems including highly oriented pyrolytic graphite (HOPG) [14, 15].

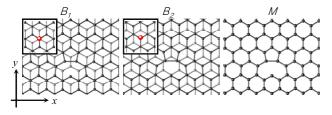
# 2. Computational details

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We perform *ab initio* calculations based on the density functional theory with spin polarization. The wavefunctions are expanded in the double- $\zeta$  basis set implemented in the SIESTA code [16]. Norm-conserving Troullier–Martins pseudopotentials are employed [17]. For the exchange–correlation term, we employ the Ceperley–Alder type [18] local density approximation with spin polarization (LSDA).  $3 \times 3 \times 1$  Monkhorst–Pack grids with respect to a  $1 \times 1$  graphene cell are used to sample the Brillouin zone and an energy cutoff for real space mesh points is 200 Ryd. All coordinates are fully relaxed until the forces of each atom

**Table 1.** Up-spin, down-spin and total charge increases in upper layers and their decreases in the lower layers of  $B_1$  and  $B_2$ .

	Charge increase in the upper layer (e)			Charge decrease in the lower layer $(e)$		
System	Total	Up-spin	Down-spin	Total	Up-spin	Down-spin
$B_1$ $B_2$	0.18 0.16	-0.01 0.00	0.19 0.16	0.18 0.16	0.07 0.06	0.11 0.10



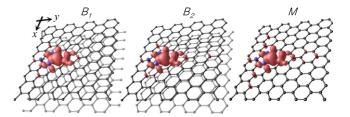
**Figure 1.** Relaxed atomic configurations of two kinds of Bernal-stacked graphene bilayers with a monovacancy labeled  $B_1$  and  $B_2$ , and of graphene monolayers with a monovacancy labeled M. Black and gray atoms represent C atoms in the upper and lower graphene layers, respectively. Insets show the site at which a C atom would be removed to generate a monovacancy before the relaxation.

are smaller than 40 meV Å $^{-1}$ . For the Bernal-stacked (AB-type) [19] graphene bilayer (composed of 255 carbon atoms) with a monovacancy, two configurations labeled  $B_1$  and  $B_2$  are considered in the supercell of  $19.68 \times 17.04$  (Å $^2$ ) with 22 Å thickness of vacuum, as shown in figure 1. For  $B_1$ , a monovacancy in the upper layer faces a C atom in the lower layer along the z direction. For  $B_2$ , on the other hand, a monovacancy in the upper layer does not face any C atom in the lower layer. The C–C bond length in one graphene sheet is  $\sim 1.42$  Å, and the interlayer distance is  $\sim 3.35$  Å. With the intention of comparison, a graphene monolayer with a monovacancy and 127 C atoms (labeled M) is also calculated. To calculate spin and charge distributions of all carbon atoms in the systems, we carry out the Mulliken population analysis [20].

# 3. Results and discussion

Each upper layer in the relaxed bilayer systems ( $B_1$  and  $B_2$ ) has nearly the same atomic arrangement as M in figure 1. The sheets are almost planar and the atoms near a monovacancy are displaced owing to the Jahn–Teller effect; for  $B_1$  and  $B_2$ , two of the three C atoms around the vacancy are rebonded with bond lengths of 1.78 and 1.79 Å, respectively. The other C atom with a dangling bond protrudes slightly toward the lower layer. The unsaturated dangling bond in  $B_2$  is somewhat closer to C atoms in the lower layer than that in  $B_1$ , so that the perturbation from the interlayer interaction may result in the total energy of  $B_2$  being lower than that of  $B_1$  by 0.03 eV, owing to the weakening of the dangling bond [5].

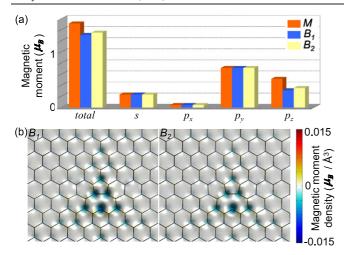
Spin (magnetic moment) densities in both  $B_1$  and  $B_2$  configurations show noticeable differences from that in M. Figure 2 shows perspective view images of isovalue density surface plots of the spin density distributions  $(\rho_{\uparrow}(r) - \rho_{\downarrow}(r))$  in  $B_1$ ,  $B_2$ , and M. Red and blue surfaces correspond to



**Figure 2.** Perspective view images of isovalue density surface plots of the spin (magnetic moment) density distributions for  $B_1$ ,  $B_2$ , and M. Red and blue colors correspond to the spin (magnetic moment) densities of + and -0.01e Å<sup>-3</sup>, respectively.

spin densities of + and -0.01e Å<sup>-3</sup>, respectively. For all three configurations, figure 2 shows that spin densities are spatially localized at the vicinity of the vacancy site and their distributions have mirror symmetry with respect to the *y*-axis. However, spin density satellites to the vacancy sites in  $B_1$  and  $B_2$  become smaller than those in M. Magnitudes of the magnetic moment in  $B_1$ ,  $B_2$ , and M manifest this difference more quantitatively. Magnetic moments in the upper and lower layers of  $B_1$ , obtained from the Mulliken population analysis [20], are 1.31  $\mu_B$ , 0.04  $\mu_B$ , and those of  $B_2$  are 1.35 and 0.04  $\mu_B$ , respectively. In comparison, the magnetic moment in M is 1.52  $\mu_B$ . This means that the magnetic moments in the upper layer of  $B_1$  and  $B_2$  decrease by 14 and 11%, respectively, compared to those in M.

To understand the origin of the reduction of the magnetic moment, the interlayer charge transfer was checked. We calculated increases in the up-spin, the down-spin, and the total charge in the upper layers and their decreases in the lower layers of bilayer systems, as listed in table 1; the charge increase in the upper layers is calculated by subtracting the total charge in M from that in the upper layers, and the charge decrease in the lower layers is calculated by subtracting the charge in the lower layers from that of the ideal graphene monolayer with 128 C atoms. For the two configurations  $B_1$ and  $B_2$ , 0.18e and 0.16e of the total charges are transferred from the lower layer to the upper layer, respectively, and most of them occupy only energy levels of the down-spin density in the upper layer, as shown in table 1. These values of the interlayer charge transfer are associated with the decrease of the magnetic moment in the upper layer of  $B_1$  and  $B_2$ , 0.21  $\mu_{\rm B}$  and 0.17  $\mu_{\rm B}$ , so that we can conclude that the reduction of the magnetic moment originates mainly from the interlayer charge transfer from the lower layer to the upper layer and their occupation of energy levels of down-spin electrons in the upper layer. For the perturbation, the missing C atom at the vacancy site is much more important than the C atom with a

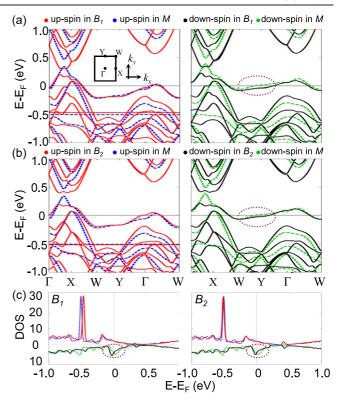


**Figure 3.** (a) Contributions of the orbitals  $(s, p_x, p_y, and p_z)$  in the C atoms in  $B_1$ ,  $B_2$ , and M to the magnetic moments. (b) Top view images of the difference in spin densities in the graphene layers with a monovacancy. Black-colored grids represent atom positions in the upper layers of  $B_1$  and  $B_2$ .

dangling bond.  $2p_z$  orbitals in upper and lower layers overlap and are associated with the interlayer interaction (coupling). Because of the missing C atom at the vacancy, the local change in the interlayer interaction occurs. For the  $B_1$  configuration, the vacancy site faces a C atom in the other graphene layer. On the other hand, for the  $B_2$  configuration, the vacancy site faces the center of a hexagon in the other graphene layer. Therefore, the charge transfer and the magnetic moment difference in  $B_1$  are somewhat larger than those in  $B_2$ .

Next, we study the influence of the interlayer charge transfer on two origins of monovacancy-induced magnetic moments: (1) the localized sp<sup>2</sup> dangling bond state from broken  $\sigma$  bonds and (2) the quasilocalized defect state from broken  $\pi$  bonds. To resolve them, we analyze contributions of the orbitals  $(s, p_x, p_y, and p_z)$  in the C atoms in  $B_1, B_2$ , and M to the magnetic moments. In figure 3(a), it is shown clearly that the difference between the magnetic moments of  $B_1$ ,  $B_2$ , and M comes from the contribution of the  $p_z$  orbital. By comparing bilayer systems ( $B_1$  and  $B_2$ ) to M, we recognize that the reduction of magnetic moments mostly originates from the quasilocalized defect state. Figure 3(b) depicts top view images of the magnetic moment density difference, cross-sectioned at the graphene layers with a monovacancy. Black-colored grids represent the upper graphene layers. The resultant distribution of spin density differences in either case is not localized at the vacancy site but has a regular triangular pattern, which corresponds to the typical pattern of magnetic moments induced by the quasilocalized defect state [4, 21]. Therefore, the interlayer charge transfer compensates for the magnetic moment induced by the quasilocalized defect state.

The situation could be more clarified with the density of states (DOS) and the band structure as shown in figures 4(a)–(c). Figures 4(a) and (b) show the comparison of band structures between  $B_1$  and M and between  $B_2$  and M, respectively. Left and right columns represent the bands of up-spin electrons and down-spin electrons, respectively. The



**Figure 4.** Band structures of  $B_1$ ,  $B_2$ , and M in the energy range from  $E_F-1$  eV to  $E_F+1$  eV in (a) and (b). Inset shows the Brillouin zone of the two-dimensional rectangular-shaped superlattice. The solid lines represent the bands of bilayer systems ( $B_1$  and  $B_2$ ) and the dotted lines represent the bands of monolayer system (M). (c) Density of states of upper layers of  $B_1$  and  $B_2$ , and M. Purple-dotted regions represent the contribution of the interlayer charge transfer to the reduction of magnetic moment in the upper layers of  $B_1$  and  $B_2$  with respect to M.

DOS of the graphene bilayer shown in figure 4(c) is calculated from the contribution of its upper layer only. Red and black colors represent the contribution of up-spin and down-spin electrons in the bilayers  $B_1$  and  $B_2$ , and blue and green represent those in M, respectively. For these three systems, we find several similar features. The band structures show that localized sp<sup>2</sup> dangling bond states are  $\sim 0.5$  eV below the Fermi energy  $(E_{\rm F})$  and quasilocalized defect states are pinned at  $E_{\rm F}$  [4]. The DOSs reveal that the magnetic moments stem mainly from the localized sp<sup>2</sup> dangling bond state, and the contributions of quasilocalized defect states are minor in all three systems. However, some differences between bilayer systems and M are also shown in these DOSs and the band structures. In contrast to M, the interlayer coupling enhances the localization character of quasilocalized defect states near the Y point below  $E_F$ , so that more down-spin states are created below  $E_{\rm F}$  (marked by a purple-dotted ellipse), resulting in occupation of transferred electrons from the adjacent layer mostly in the down-spin quasilocalized defect state. The DOS of down-spin electrons shows this tendency more clearly. The main peak position in the DOS of the down-spin quasilocalized defect state in the bilayer systems moved from above  $E_{\rm F}$  to below  $E_{\rm F}$  with respect to M, and the quasilocalized defect state below  $E_{\rm F}$  of the bilayer systems has less dispersive band than that of M, demonstrating an enhancement of the localization character of the bilayer system. The band dispersion in the band structure can show localization character. It means that a flat band corresponds to a localized state. Therefore less dispersive (flatter) bands are associated with quasilocalized states with heavy effective masses. Similar to the case of downspin electrons, the band structure of the up-spin quasilocalized defect state in the bilayer becomes more localized near the Y point, compared to M. However, the band of the up-spin quasilocalized defect state near Y is far below  $E_{\rm F}$ , so that there is little increase in the DOS of up-spin electrons of the quasilocalized defect state from the interlayer charge transfer. Consequently, enhancement of the localization character of quasilocalized defect states near the Y point below  $E_{\rm F}$  and occupation of transferred electrons from the adjacent layer in the down-spin quasilocalized defect state are the major factors that contribute to the reduction of magnetic moments. Other bands in the bilayer system are also affected by the interlayer coupling in the graphene bilayer, but their contribution to the magnetic moment is negligible.

## 4. Conclusion

In conclusion, we demonstrated, by *ab initio* calculations, that the interlayer charge transfer to a down-spin quasilocalized defect state with enhanced localization character results in the reduction of the magnetic moment of the total magnetic moment in graphene bilayers. Our study sheds light on the physical behavior of sp²-bonded carbon structures with vacancies and may lead to a new avenue of carbon-based spintronics.

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